

MM2EMD SOLUTIONS

Q1. $1/C_{eq} = 1/47 + 1/(10+33) = 0.044 \mu F^{-1}$ [1]

So $C_{eq} = 22.45 \mu F$ [1]

$Q = CV = 10 \times 22.45 \times 10^{-6} = 2.245 \times 10^{-4} C$ [1]

2) $Z = 15 + j2\pi \times 50 \times 0.03 = 15 + j9.32 \Omega$ [1]

$I = 20/(15 + j9.32) = 20 \times (15 - j9.32) / (15^2 + 9.32^2)$

$= 0.96 - j0.60 A$ [2]

$= 1.13 A \angle -31.2^\circ$ [1]

$V = 15 \times (0.96 - j0.60) = 14.4 - j9V = 15.95 V \angle -31.2^\circ$ [2]

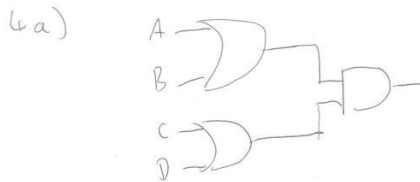
3) $Z_{ref} = Z \times (n_1/n_2)^2 = (7 + j3) \times 3^2 = 63 + j27 \Omega$ [2]

which has a magnitude of 67.8Ω [1]

4. AC+AD+BC+DB [1]

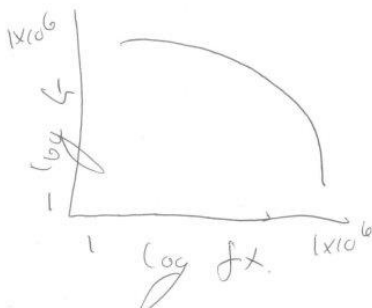
D.C [1]

A.B.C [1]



Appropriate circuits [1] each.

5. i) Marks, for high gain at DC, low gain at high frequency, correct scales, use of log scale. [5]



ii) Saturation and non linear gain. [3]

6. $\log(4 \times 10^{12}) / \log(2) = 42$ [4] (award 0 marks for a decimal number)

7 (a) $n_s = 60f/p = 60 \times 50/2 = 1500 \text{ rev/min}$ [1 for approach 1 for correct ans]

(b) $V_p = VL/\sqrt{3} = 415/1.73 = 239.6 \text{ V}$ [1 for approach 1 for correct ans]

(c) $s = (1500-1445)/1500 = 0.03667$ [1]

$a = 4/20 = 0.2$ [1]

$$T = \frac{3p}{2\pi f} \times \frac{V^2 a s}{X_R (a^2 + s^2)}$$

$$= \frac{3 \times 2}{2\pi \times 50} \times \frac{239.6^2 \times 0.2 \times 0.0367}{20(0.2^2 + 0.0367^2)} = 9.72 \text{ Nm}$$

[1 for method, 2 for correct numbers, 1 for answer]

Power = $T\omega = 9.72 \times 1445 \times 60 / (2 \times \pi) = 1470 \text{ W}$ [1 for method, 1 for answer]

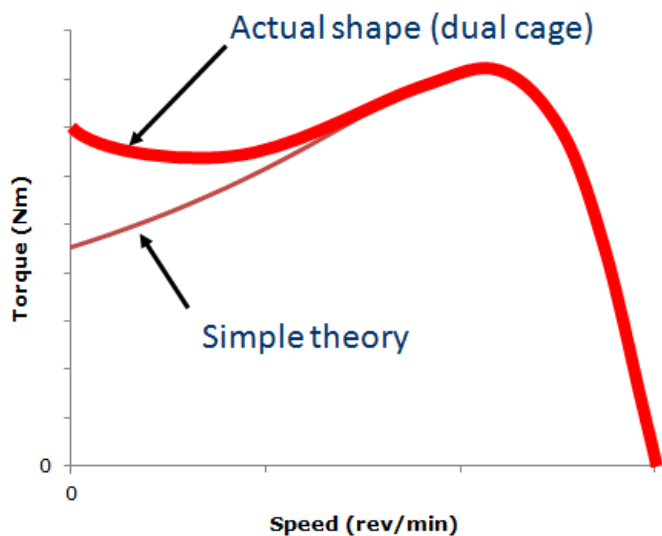
d) At stall, $s=1$ [1]

$$T = \frac{3p}{2\pi f} \times \frac{V^2 a s}{X_R (a^2 + s^2)}$$

$$= \frac{3 \times 2}{2\pi \times 50} \times \frac{239.6^2 \times 0.2 \times 1}{20(0.2^2 + 1^2)} = 10.54 \text{ Nm}$$

[1 for method, 1 for numbers, 1 for ans]

Torque likely to be more in practical motor as deep bar or dual cage rotor often used [1]



[2 for correct shapes, 2 for axes and labels]

e) Electrical power = $3 V_p I_p \cos \phi = 3 \times 239.6 \times 3.25 \times 0.68 = 1588 \text{ W}$ [3]

Efficiency = mechanical output/electrical input = $1470/1588 = 0.925 = 92.5\%$ [2]

f) Three phase supply results in rotating magnetic field inside stator [2]

This causes relative motion between field and rotor [1]

This causes current to flow in conductors in rotor [2]

Current in conductors causes them to be experience force [1] – the bigger the current, the more drag [1]

Force causes rotor to be dragged around by rotating magnetic field [1]– the bigger the relative motion, the more torque drags rotor around [1]

(Use discretion on marks)

8(a) $I=V/R = 100/25=4$ [2] so MMF = $NI = 800*4=3200$ A-turns [2]

b) Assume negligible reluctance in core compared with air gaps so MMF is all across gaps [2]; also uniform flux across each gap [1]. Total gap length is 0.02 m.

$H=NI/l=3200/0.02 = 160000$ A/m [3]

Air so $\mu=\mu_0\mu_r \approx \mu_0$ [2] so $B=\mu_0 H = 4\pi \times 10^{-7} \times 160000 = 0.2T$ [2]

Per pair of poles: $F=B^2A/(2\mu_0) = 0.2^2 \times 0.005 / (2 \times 4\pi \times 10^{-7}) = 79.6N$ [2]

So total lifting force = $2F = 2 \times 79.6 = 159.2$ N [2]

c) $H=NI/l = 3200/0.4=8000$ A/m [3]

From graph $B=1.8T$ [2]

Per pair of poles: $F=B^2A/(2\mu_0) = 1.8^2 \times 0.005 / (2 \times 4\pi \times 10^{-7}) = 6445$ N [2]

So total lifting force = $2F = 2 \times 6445 = 12891$ N [2]

Assumes uniform flux across each gap [2] and negligible air gaps so neglect reluctance of air gaps. [2]

d) Pneumatic cylinder [2] operated by solenoid valve [2]. This requires a transistor or similar device [2] to amplify the logic signal, probably with a resistor and a power supply [1].

9.

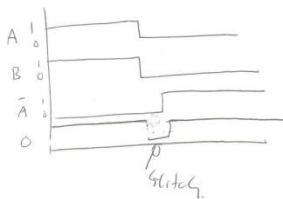
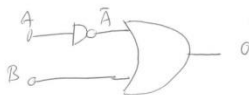
a.

A	B	C	O
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

[4 marks]

A circuit [3] that looks like $ABC+ABC'+AB'C$ [3 marks]

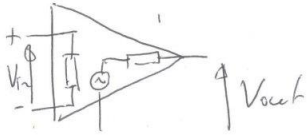
b. Race times are caused by digital components taking a finite time to respond to a change in input.



[2 marks]

A good example would be the timing diagram of the following circuit AB' [3 marks]

c. Marks for a diagram [2] with the input resistance [1], output resistance [1] and all terminals visible and labelled [1].

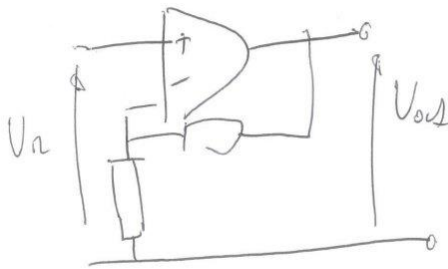


$$V_{out} = V_{in} A_v$$

$$R_{out} = 0 \Omega$$

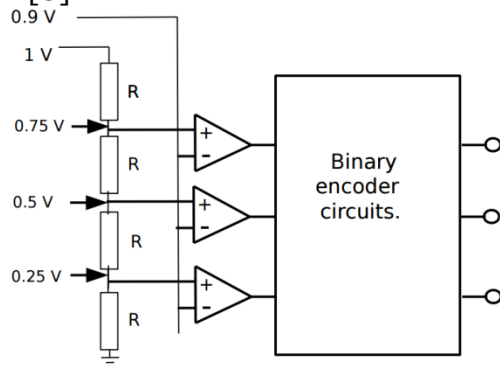
$$R_{in} = \infty \Omega$$

d. *Marks for correctly drawn non-inverting op-amp [3]



- *Any correct derivation of the closed loop gain expression [2].
- *Assumptions: $V_- = V_+$. [1]
- *Any sensible values that make $A = 1 + R_f/R_g$ go to 10. [1]

e. Flash converters don't need to count up and are therefore faster. [2]
Diagram [3]

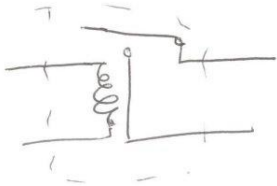


f. $20/2^2$

[3 marks]

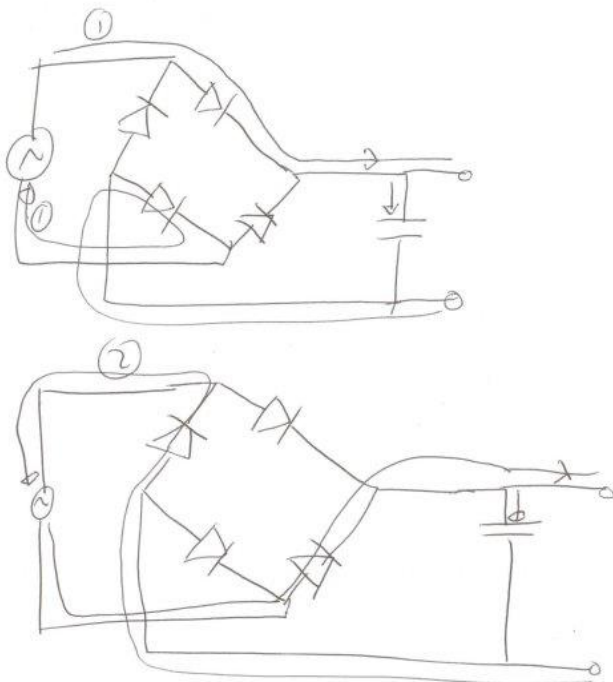
10.

- a. The diagram must have a coil and a switch in it. [3] The advantages are electrical isolation [1] but the disadvantages are high power consumption and slow switching speed. [1]



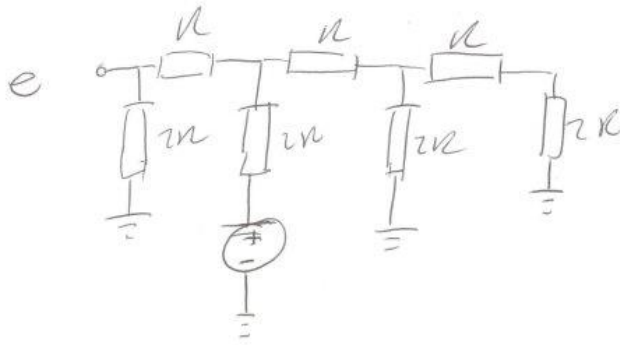
- b. The diagram must have show charge being present/absent in a channel. [2] The slow switching speed is due to the need to charge and discharge the gate which is a bit like a capacitor. [3]

- c. A correct diagram of a bridge rectifier [5], with a capacitor [1] and arrows showing how charge flows during the charge/discharge cycles, for both negative and positive. [4]



- d. $100\text{mA}/(50 \times 0.1) = 0.02 \text{ F}$ [3]. Use a voltage regulator. [2]

- e. A correct diagram of a 4bit R2R ladder [5].



0.5 V would appear on the output [1]. A very good attempt simplifying the R2R ladder circuit to prove the output would be 0.5 V [4].