

# The University of Nottingham

DEPARTMENT OF MECHANICAL, MATERIALS AND MANUFACTURING ENGINEERING

A LEVEL 2 MODULE, SPRING SEMESTER 2020-2021

## ELECTROMECHANICAL DEVICES

Time allowed TWO hours

Answers/mark scheme:

### Q1.

A1	A0	B1	B0	Q3	Q2	Q1
0	0	0	0	0	0	0
0	0	0	1	0	0	1
0	0	1	0	0	1	0
0	0	1	1	0	1	1
0	1	0	0	0	0	1
0	1	0	1	0	1	0
0	1	1	0	0	1	1
0	1	1	1	1	0	0
1	0	0	0	0	1	0
1	0	0	1	0	1	1
1	0	1	0	1	0	0
1	0	1	1	1	0	1
1	1	0	0	0	1	1
1	1	0	1	1	0	0
1	1	1	0	1	0	1
1	1	1	1	1	1	0

5 marks for a fully correct answer.

3 marks for minor errors.

0 marks for multiple errors.

**Q2.**  $G = -R_f A / (R_f(A+1) + R_i)$

$$\text{Gain} = -1 \times 10^4 \times 5 \times 10^3 / (1 \times 10^3 \times (5 \times 10^3 + 1) + 1 \times 10^4)$$

$$\text{Gain} = -9.9780$$

3 marks for the correct answer.

0 marks for anything else, including missing the minus.

Op-Amps are not used in their open loop configuration because the gain is too high to be useful.[2]

**Q3.**  $1 \times 10^{-3} = (5V - 5V) / 2^n$

$n = 14$  bits. [3]

**Q4**

Equivalent resistor for the paralleled circuit  $R_1 // R_2 = 5$  Ohms [1]

Equivalent resistor for total is  $R_{\text{eff}} = R_1 // R_2 + R_3 = 15$  ohm [1]

Thus the current  $I = V / R_{\text{eff}} = 30V / 15\text{ohm} = 2A$  [1]

The power dissipated by the network is  $P = I^2 R_{\text{eff}} = 4 * 15 = 60W$  [2]

**Q5**

$$Z = R + jX_L = 200 + j * 2\pi * 400 * 100e-3 = 200 + j251 \quad [1]$$

$$|Z| = \sqrt{R^2 + X_L^2} = 321 \text{ Ohm} \quad [1]$$

The power factor  $\text{Pf} = \cos(\phi) = R / |Z| = 200 / 321 = 0.623$  [1]

$$I_{\text{rms}} = V_{\text{rms}} / |Z| = 115 / 321 = 0.36A \quad [1]$$

The power dissipated by the load

$$P = V_{\text{rms}} I_{\text{rms}} * \text{Pf} = 115 * 0.36 * 0.623 = 27.8W \quad [1]$$

**Q6**

Using the  $V_1 / V_2 = N_1 / N_2$

The secondary side voltage  $V_2 = N_2 / N_1 * V_1 = 100 / 1000 * 240V = 24V$  [1]

Second side current  $I_2 = V_2 / R_L = 24 / 2 = 12A$  [1]

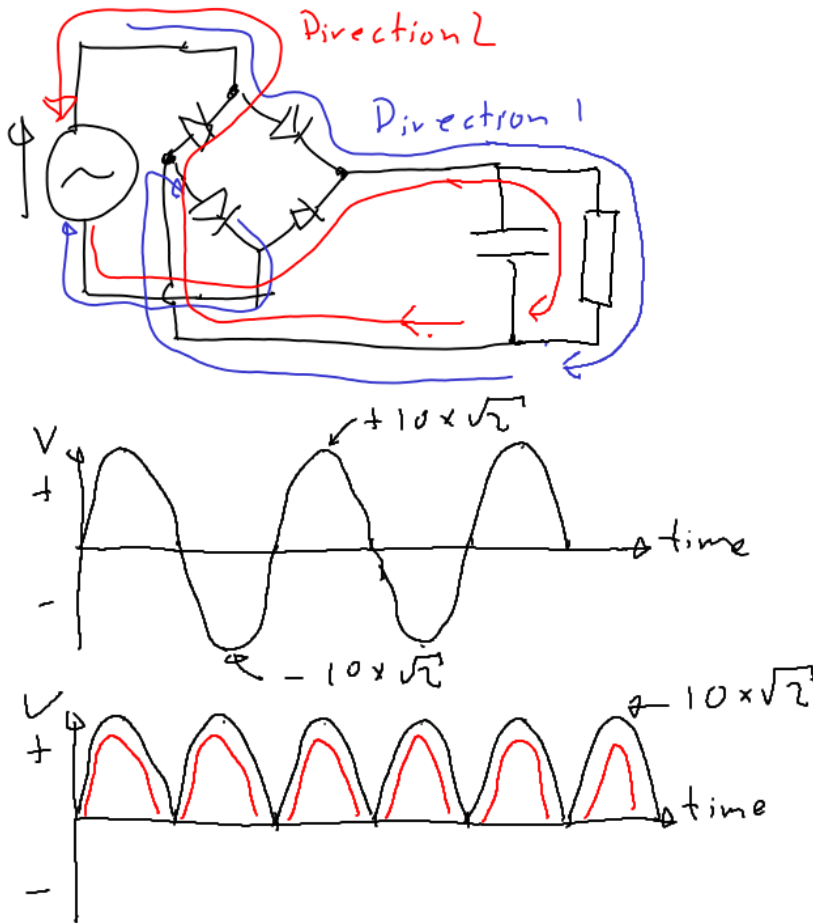
The primary side current thus using  $V_1 I_1 = V_2 I_2$

$$I_1 = V_2 I_2 / V_1 = 24 * 12 / 240 = 1.2A \quad [1]$$

The equivalent resistance seen by the AC power supply is equal to  $R = V_1 / I_1 = 240V / 1.2A = 200 \text{ Ohm}$

A flash converter is faster than an R2R ladder. [2]

Q7a.



5 marks for the correct bridge rectifier, with arrows.  
 3 marks for correct input/output waveform, with magnitudes.  
 2 marks for the diode losses (red line).

Q7b.

$$V_{\text{ripple}} = I/fC$$

$$C = 1.0 / (1 \times 10^{-4} \times 50)$$

$$C = 200F. [1]$$

No this is not a reasonable at all, the capacitor would be too big. [1]

A voltage regulator could also be used to reduce the ripple. [1]

Q7c.

$$(0.6 \times 2 \times 1.0) \text{ Watts}$$

[2]

Q7d.

a	b	c	Q
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0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

$$Q = abc + abc + abc + abc$$

3 marks for the table.

2 marks for the expression.

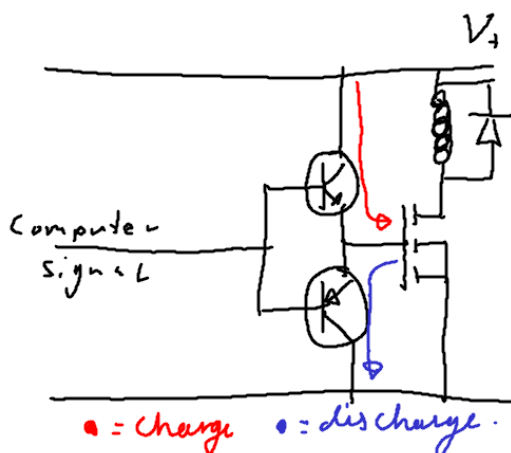
Q7e.

$$\begin{aligned}
 Q &= \bar{a} \bar{b} \bar{c} + \bar{a} b \bar{c} + a \bar{b} \bar{c} + a b \bar{c} \\
 &= \bar{a} (\bar{b} \bar{c} + b \bar{c}) + a (\bar{b} \bar{c} + b \bar{c}) \\
 &= \bar{a} \bar{c} (\bar{b} + b) + a \bar{c} (\bar{b} + b) \\
 &= \bar{a} \bar{c} + a \bar{c}
 \end{aligned}$$

3 marks for the correct answer.

2 marks for the method.

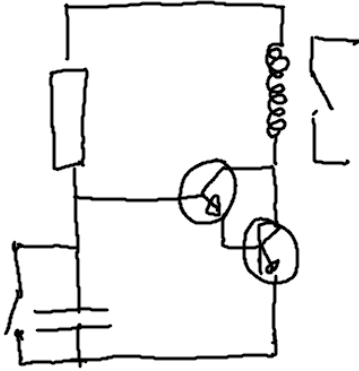
Q7f.



3 marks for the diagram. Deduct 1 mark for each mistake.

2 marks for: The use of the push pull pair enables fast charging/discharging of the MOSFET.

Q7g.



$$V(t) = V_{\max}(1 - \exp(-t/\tau))$$

$$2/3 = 1 - \exp(-t/\tau)$$

$$1/3 = \exp(-t/\tau)$$

$$\ln(1/3) = -t/\tau$$

$$-\tau \ln(1/3) = t$$

$$t = 10.987 \text{ seconds.}$$

Q8.

- (a) The motor is with 4 poles thus 2 pole pairs,  $p = 2$  [1]. The synchronous speed of the motor  $N_s = 60 \cdot f/p = 60 \cdot 50/2 = 1500 \text{ rpm (rev/min)}$  [2]
- (b) The line-to-line voltage  $V_{LL} = 415\text{V}$ , thus the phase voltage  $V_p = V_{LL}/\sqrt{3} = 239.6\text{V}$  [3 marks, 1 for approach and 2 for correct answer]
- (c) The slip at the rated speed  $s = (N_s - N)/N_s = (1500 - 1445)/1500 = 0.0367$  [2]  
 $a = 2/10 = 0.2$  [1]

c.  $a = 0.2$

$$T = \frac{3P}{2\pi f} \cdot \frac{V^2 a s}{X_R(a^2 + s^2)} = \frac{3 \times 2}{2\pi \times 50} \cdot \frac{239.6^2 \cdot 0.2 \cdot 0.0367}{10(0.04 + 0.001367)}$$

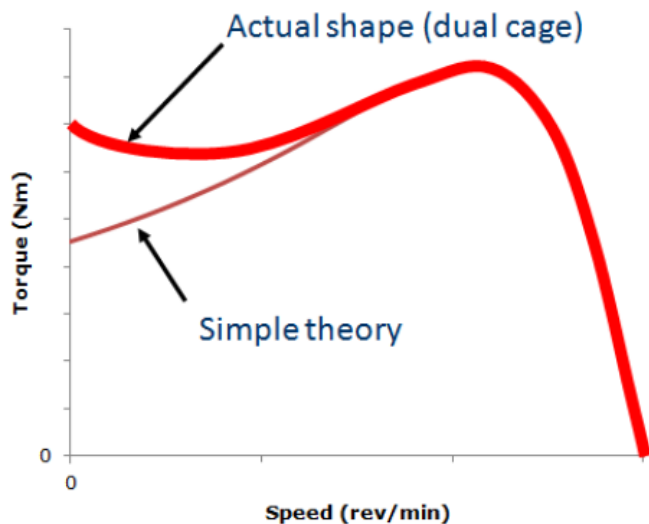
$$= 19.46 \text{ Nm [3]}$$

$$P = T \omega = 19.46 \cdot 1445 \cdot \frac{2\pi}{60} = 2944.7 \text{ W [2]}$$

d.  $s = 1$  (~~0.0367~~)

$$T = \frac{3P}{2\pi f} \cdot \frac{V^2 a s}{X_R(a^2 + s^2)} = 21.28 \text{ Nm}$$

d) continued: Starting torque is higher than rated torque [1]. Torque is likely to be more in practical motor as deep bar or dual cage rotor often used



[2 for correct shape and 2 for axel lables]

e) Electrical power  $= 3 V_p I_p \cos \phi = 3 \times 239.6 \times 6.5 \times 0.68 = 3177\text{W}$  [3] Efficiency = mechanical output/electrical input =  $2944.7/3177 = 0.927 = 92.7\%$  [2]

f) Three phase supply results in rotating magnetic field inside stator [2]

This causes relative motion between field and rotor [1]

This causes current to flow in conductors in rotor [2]

Current in conductors causes them to be experience force [1] – the bigger the current, the more drag [1]

Force causes rotor to be dragged around by rotating magnetic field [1]– the bigger the relative motion, the more torque drags rotor around [1]