

**MM2MS2 - Mechanics of Solids 2**  
**Exercise Sheet 3 – Thermal Stress and Strain**

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1. An unrestrained steel bar of length 80 mm is heated from 20 °C to 50 °C, determine the change in length of the bar.  $\alpha = 11 \times 10^{-6} \text{ } ^\circ\text{C}^{-1}$  for steel.  
**[Ans.: 0.0264 mm]**
2. If the bar in Q1 has a Young's modulus of 200 GPa and is restrained from expanding axially, determine the stress in the bar.  
**[Ans.: -66 MPa]**
3. The bolt and sleeve assembly shown in Figure Q3 is initially tightened so that there is no pre-stress at a temperature of 20 °C. The temperature of the assembly is increased to 70 °C. Determine the total extension of the assembly and the stress in the sleeve and the bolt if the bolt is made of steel with a cross-sectional area of 85 mm<sup>2</sup> and the sleeve of aluminium with a cross-sectional area of 235 mm<sup>2</sup>.  $\alpha = 11 \times 10^{-6} \text{ } ^\circ\text{C}^{-1}$  and  $E = 200 \text{ GPa}$  for steel and  $\alpha = 23 \times 10^{-6} \text{ } ^\circ\text{C}^{-1}$  and  $E = 70 \text{ GPa}$  for aluminium.  
**[Ans.: extension: 0.084 mm; bolt stress: 59 MPa; sleeve stress: -21 MPa]**

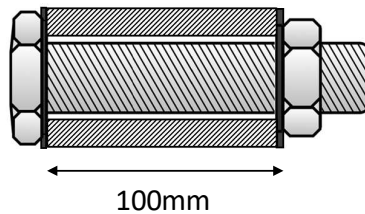


Figure Q3

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4. The 50-mm-diameter central cylinder shown in Figure Q4 is made from aluminium ( $\alpha = 23 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  and  $E = 70 \text{ GPa}$ ) and is placed in the clamp when the temperature is  $T_1 = 20^\circ \text{C}$ . If the two steel ( $\alpha = 11 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  and  $E = 200 \text{ GPa}$ ) bolts of the clamp each have a diameter of 10 mm, and hold the cylinder snug with negligible force against the rigid jaws at  $T_1$ , determine the stress in the cylinder when the temperature rises to  $T_2 = 100^\circ \text{C}$ .

**[Ans.: -6.83 MPa]**

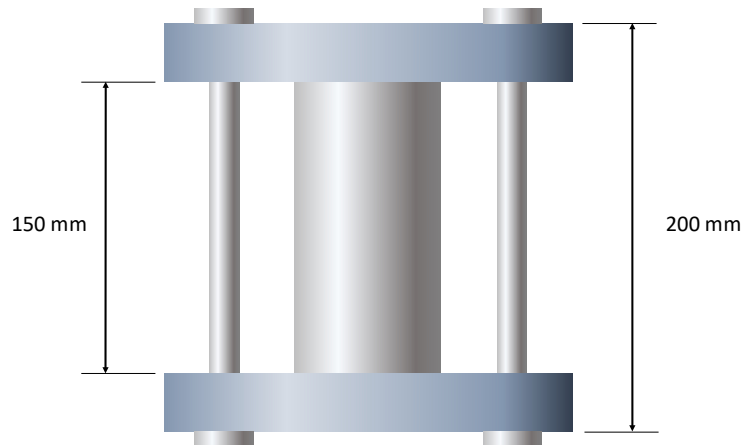


Figure Q4

5. An unrestrained rectangular section aluminium beam with the cross-sectional dimensions shown in Figure Q5, has a temperature profile given by:

$$\Delta T = 50 \left( 1 - \frac{4y^2}{40^2} \right)$$

Plot the stress distribution and determine the maximum tensile stress in the bar. For aluminium,  $\alpha = 23 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  and  $E = 70 \times 10^9 \text{ GPa}$ .

**[Ans.: 53.7 MPa]**

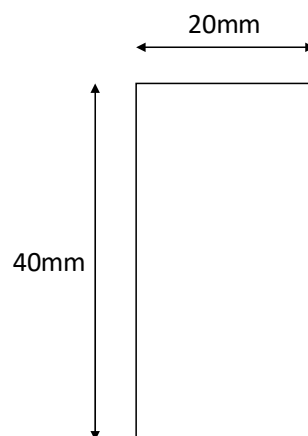


Figure Q5