

MM2MSD – Mechanics of Solids 2

Exercise Sheet 1 – Combined Loading

1. In an experiment involving the behaviour of a thin wire of 0.25mm diameter, a mass of 5 kg is suspended from the wire and a torque of 1.72 mNm is applied. Calculate the in-plane principal stresses and the maximum shear stress for this case.

[Ans.: $\sigma_1 = 1250.5 \text{ MPa}$, $\sigma_2 = -251.3 \text{ MPa}$, $\tau_{max} = 751 \text{ MPa}$]

2. A thin-walled cylindrical tank is subjected to an internal pressure of 300 kPa and a torsional moment of 15kNm. The outer radius of the tank is 250 mm and the wall thickness is 1 mm. Calculate

- i) the in-plane principal stresses and the maximum in-plane shear stress
ii) the overall maximum shear stress for the stress system

[Ans.: i) $\sigma_1 = 98.95 \text{ MPa}$, $\sigma_2 = 13.55 \text{ MPa}$, $\tau_{max} = 42.7 \text{ MPa}$;

ii) $\tau_{max} = 49.48 \text{ MPa}$]

3. A helicopter rotor shaft, 50mm in diameter, transmits a torque of 2.4 kNm and an upward tensile lifting force of 125 kN. Determine the maximum tensile stress, maximum compressive stress and maximum shear stress in the shaft.

[Ans.: $\sigma_1 = 134.6 \text{ MPa}$, $\sigma_2 = -71 \text{ MPa}$, $\tau_{max} = 102.8 \text{ MPa}$]

4. A generator shaft of hollow circular cross-section is subjected to a torque of 25 kNm and a compressive load of 900 kN. The outer and inner diameters of the shaft are 200 mm and 160 mm respectively. Determine the in-plane principal stresses and maximum shear stress.

[Ans.: $\sigma_1 = 8.3 \text{ MPa}$, $\sigma_2 = -87.9 \text{ MPa}$, $\tau_{max} = 48.1 \text{ MPa}$]

5. For the purpose of analysis, a segment of a crankshaft in a vehicle is presented as shown in Figure Q5. The load $P = 1 \text{ kN}$, and the dimensions are $b_1 = 80 \text{ mm}$, $b_2 = 120 \text{ mm}$ and $b_3 = 40 \text{ mm}$. The diameter of the shaft is $d = 20 \text{ mm}$. Determine the maximum tensile, compressive and shear stresses at point A, located on the surface of the shaft at the z-axis.

[Ans.: $\sigma_1 = 31.6 \text{ MPa}$, $\sigma_2 = -184.6 \text{ MPa}$, $\tau_{max} = 108.1 \text{ MPa}$]

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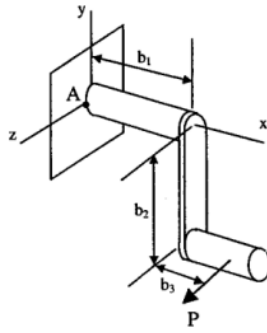


Figure Q5